



Illustrative Multivariate Visualization for Geological Modelling

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Usman R. Alim*, and Mario Costa Sousa*

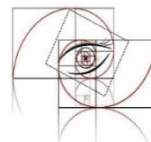
* Department of Computer Science

** Department of Geoscience



VISAGG

Visualization and Graphics Group



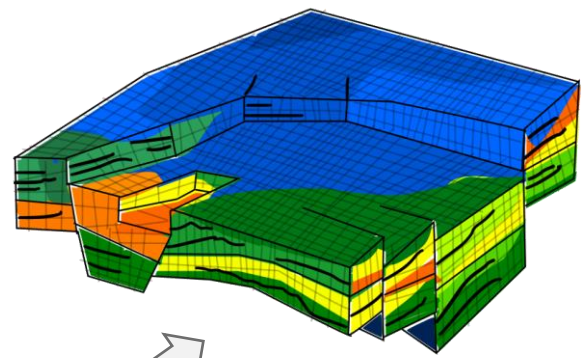
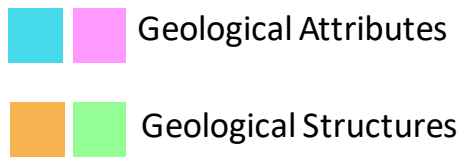
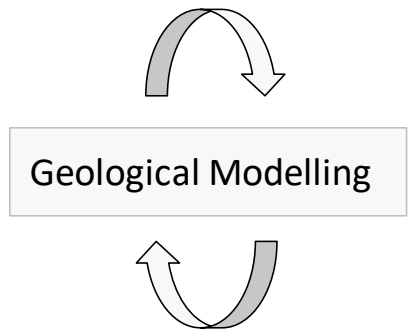
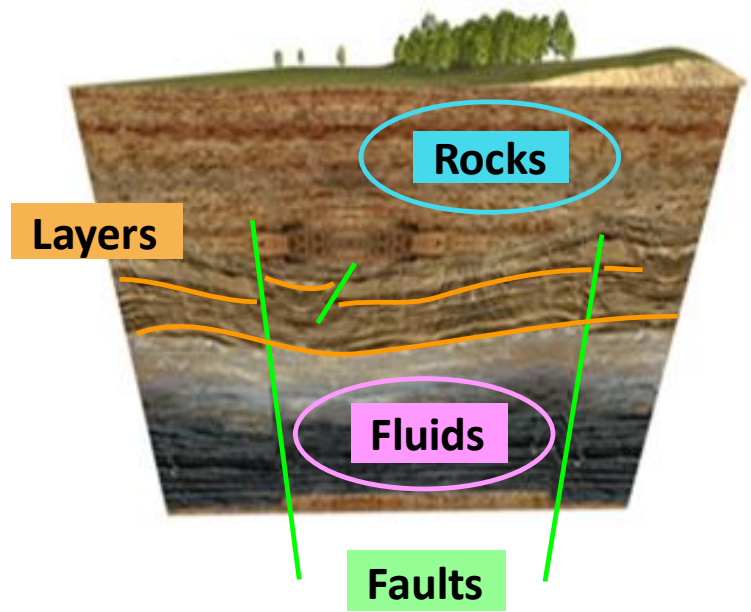
illustrares

Interactive Modeling, Visualization
& Analytics R&D Group



Geological Modelling

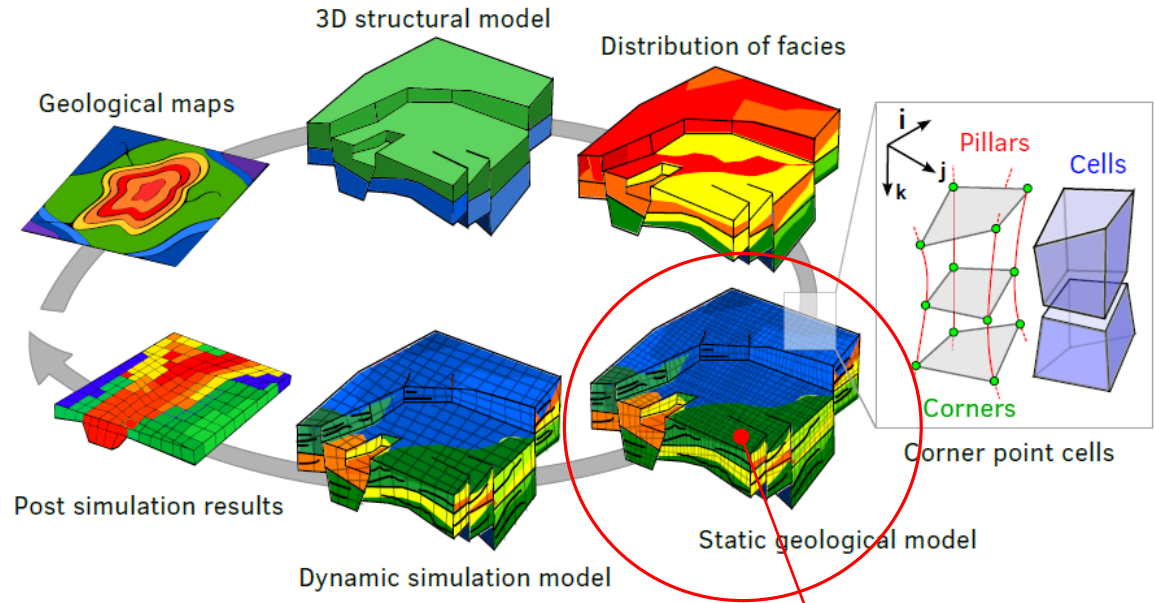
- Process to create a digital representation of the underground reservoir



Geological model



Geological Models



Data Analysis

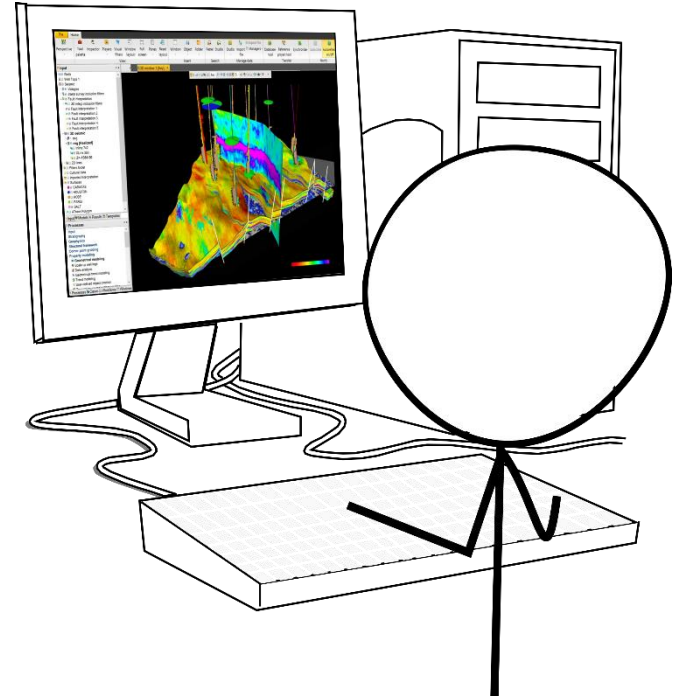
- Geological distributions
- Correlation between attributes
- Connected areas
- Possible flow trajectories

- rock type
- porosity
- permeability
- oil saturation



Conventional Visualization

- Don't consider data type
- Colormaps (rainbow)
- Difficult to correlate attributes
- Difficult to understand internal structures
- Difficult to communicate results

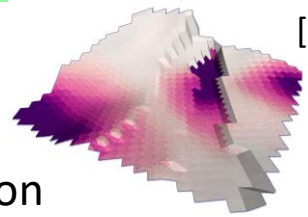




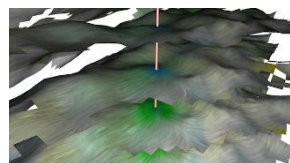
Related Work

Multivariate Visualization

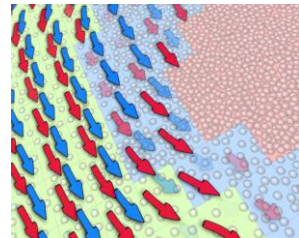
- Noise texture + Colormaps
 - 1 or 2 attributes
- **Decal-Maps**



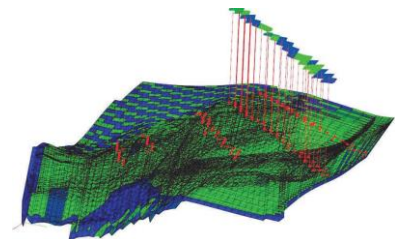
[Höllt et al., *EnvirVis* 2016]



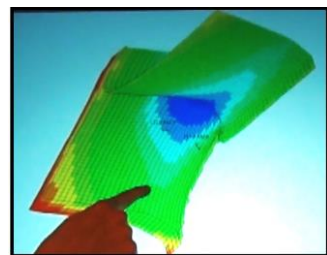
[Toledo et al., *SIBGRAPI* 2011]



[Rocha et al., *TVCG* 2017]



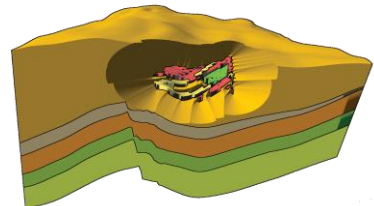
[Somanath et al., *GI* 2014]



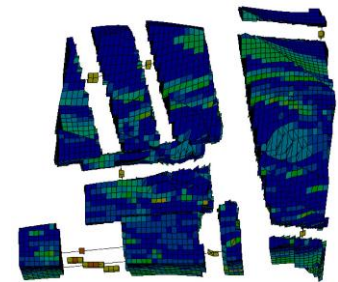
[Sultanum et al., *ITS* 2011]

• Illustrative Visualization (*what*)

- Cutaways
- Exploded View
- Peeling



[Lidal et al., *SCCG* 2012]



[Martins et al., *SIBGRAPI* 2012]



Our approach – *how* to visualize

- Expressive visualization of static geological attributes
- Highlight 3D structures, in particular possible connected areas
- Superimposed visualization of multiple attributes



Task Analysis and Goals

- Problem Domain Characterization
 - *Multi-level typology framework* [Brehmer *et al.*, TVCG 2013]
- Tasks
 - Discover geological scenarios***
 - **T1** – *Explore* areas of low/high magnitude, and/or strong/weak directionality.
 - **T2** – *Identify* correlations between static properties through *comparison*.
 - **T3** – *Explore* the distribution of properties to *identify* connected regions
 - Verify possibilities of flow behavior***
 - **T4** – *Explore* the properties to *identify* correlations with dynamic behavior
 - Present the results***
 - **T5** – *Look up* geological properties and *summarizing* trends



Task Analysis and Goals

- Design Goals
 - **DG1:** *Suitable representation of geological attributes.*
 - **DG2:** *Facilitate communication between multidisciplinary teams.*
 - *“(Managers) don’t care about (cell-specific values), they just want to know ‘where is the oil’, ‘what is it doing there’, ‘what is going to cost us to get it out’” [Sultanum et al., 2011]*
 - **DG3:** *Facilitate visualization of trends.*
 - *“I am looking through specific trends and not through one specific value”. [Sultanum et al., 2011]*
 - **DG4:** *Display of multiple attributes.*
 - **DG5:** *Access the 3D nature of geological models.*



Visualization Design

- Surface representation
 - Colormaps + decal-maps
- 3D representation
 - 3D glyphs
- We draw inspiration from Perception, InfoVis and Traditional Illustration



Visualization Design – Surface representation

- Rock type (categorical data)
 - 2-4 rock types
 - Representation *pastel colormap*



- Avoid pastel blue tone
- Oil Saturation (scalar data)
 - Pastel tone (rock type) + *brightness* variation



Visualization Design – Surface representation

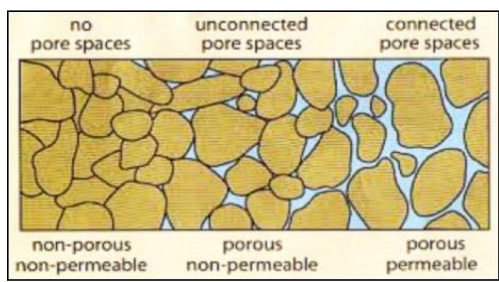
- Porosity (scalar data)

- Volumetric value given by the ratio:

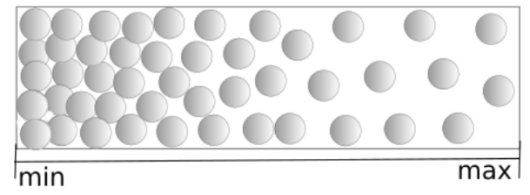
$$\phi = \frac{V_v}{V_t}$$

V_v Is the void-space

V_t is the total volume



[Rocha *et al.*, TVCG 2017]



Poisson importance sampling



Grain decal



Visualization Design – Surface representation

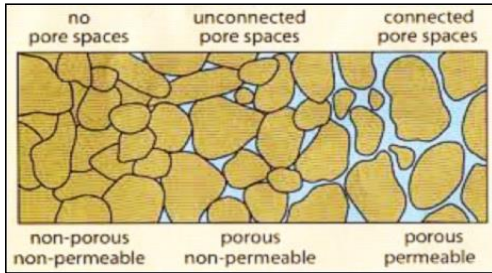
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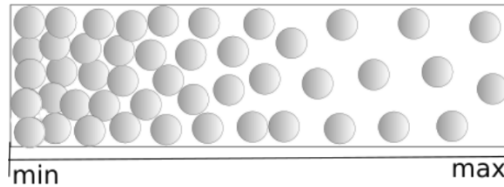
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Poisson importance sampling



Grain decal

Costly to compute for arbitrary grids

Does not consider local control over the distribution



Visualization Design – Surface representation

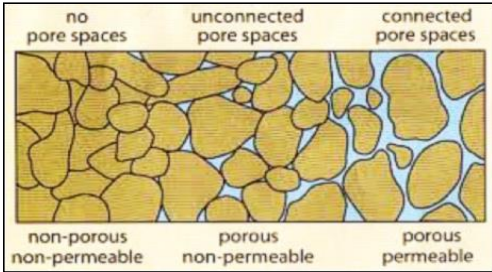
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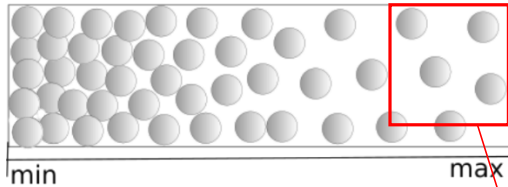
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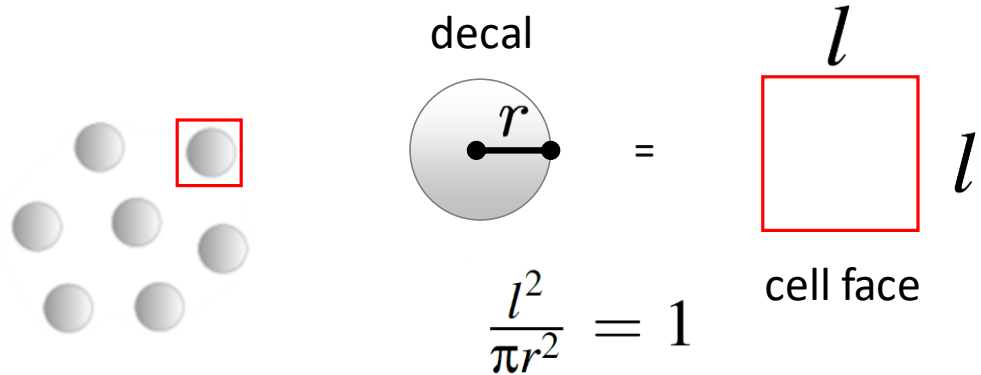
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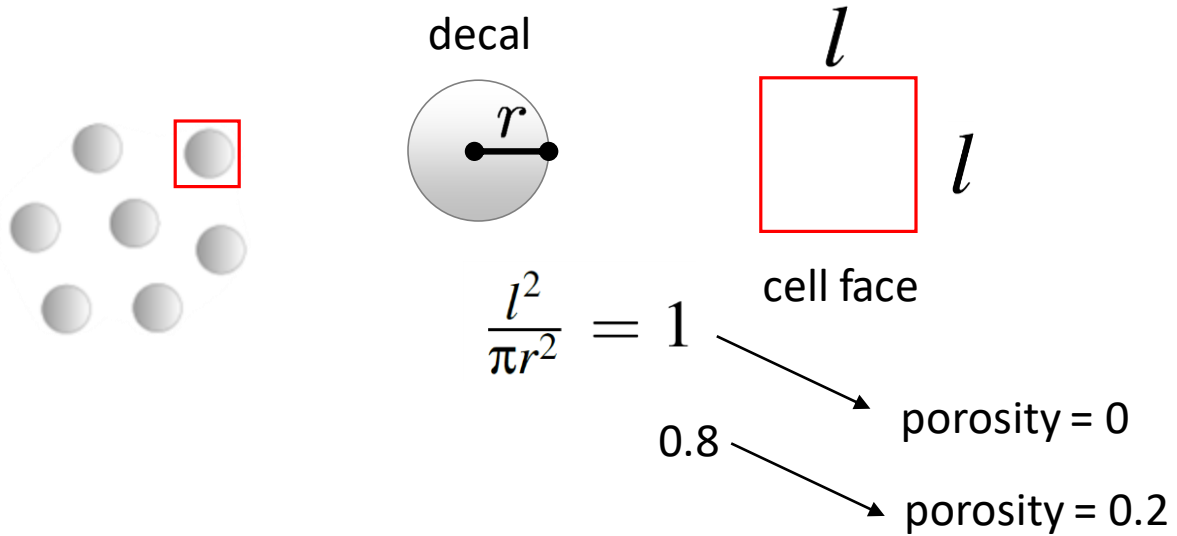
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Visualization Design – Surface representation

- Porosity (scalar data)





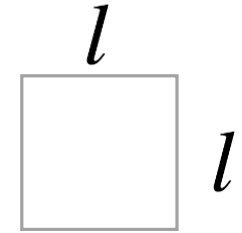
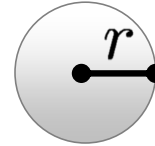
Visualization Design – Surface representation

- Porosity (scalar data)

$$l_u(p) := r\sqrt{\pi(1-p)}, \text{ where } 0 \leq p \leq 1$$

where p is the porosity value.

decal



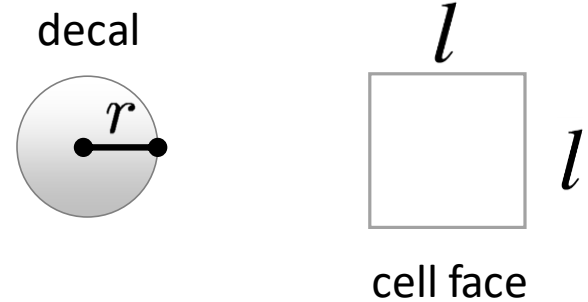
cell face

$$\frac{l^2}{\pi r^2} = 1 - p$$



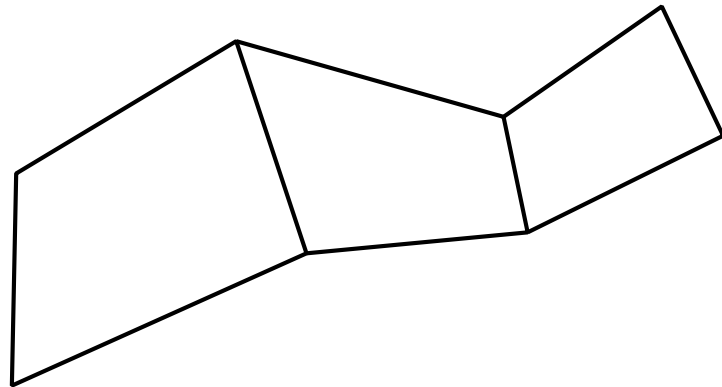
Visualization Design – Surface representation

- Porosity (scalar data)
 - Importance sampling strategy
 - Sampling **per cell face** of the reservoir grid



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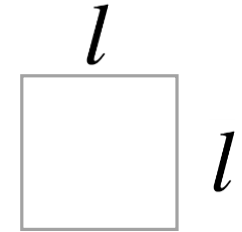
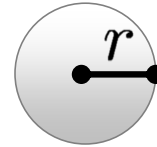
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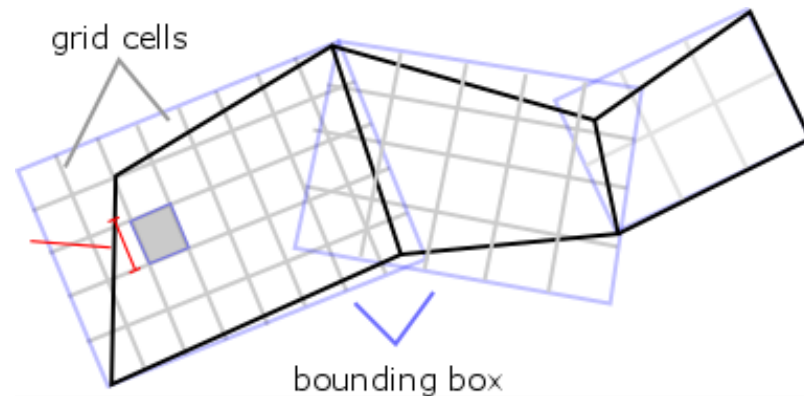
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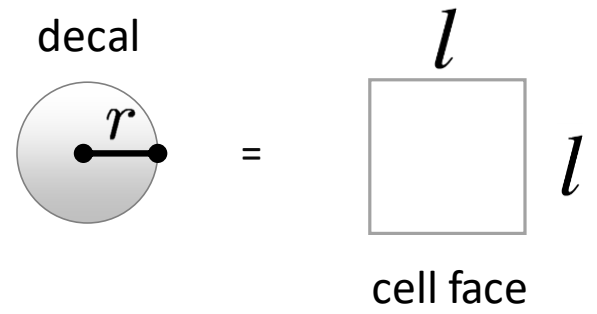
cell face





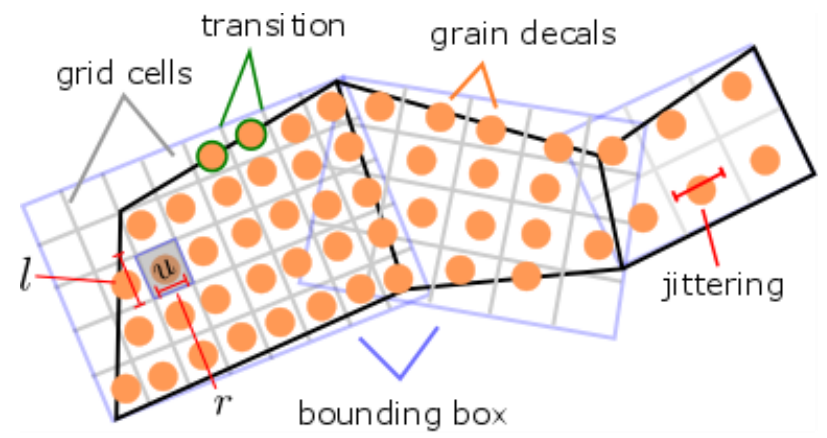
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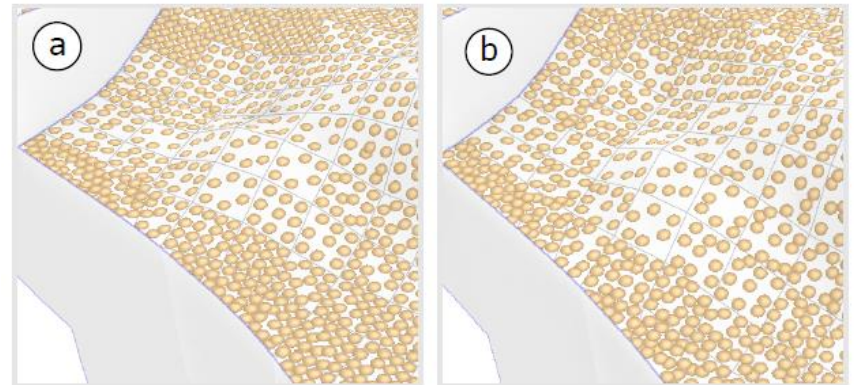
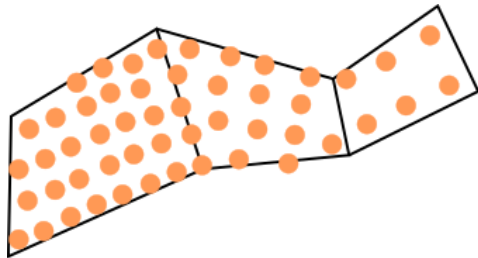
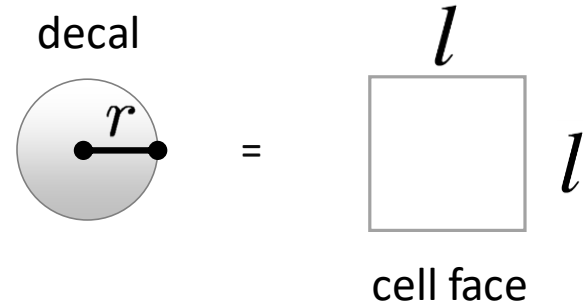


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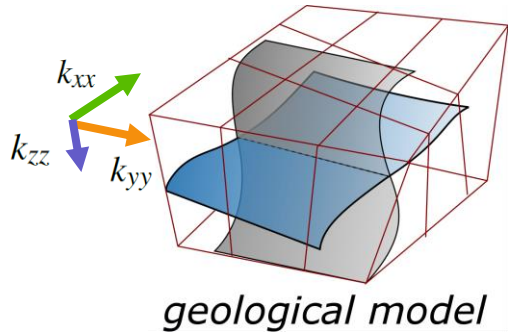
Visualization Design – Surface representation

- Rock Permeability (tensor data)
 - Measures the ability of the medium support fluid flow
 - Represented as a diagonal 3x3 matrix (k_{xx}, k_{yy}, k_{zz})



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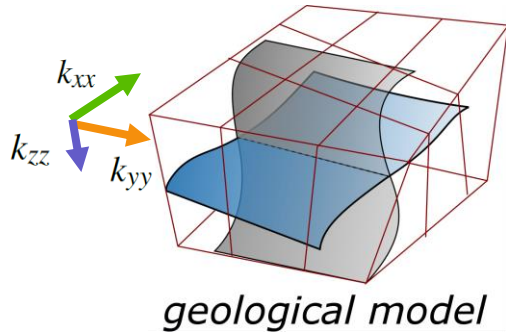


$$k_{xx} \cong k_{yy} \gg k_{zz}$$



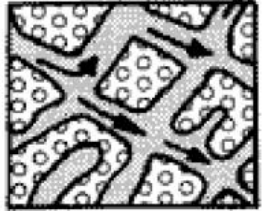
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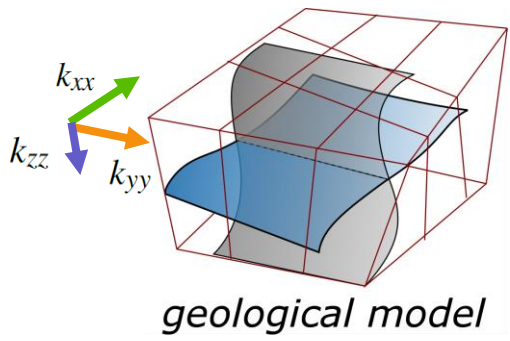
PERMEABLE
ROCK



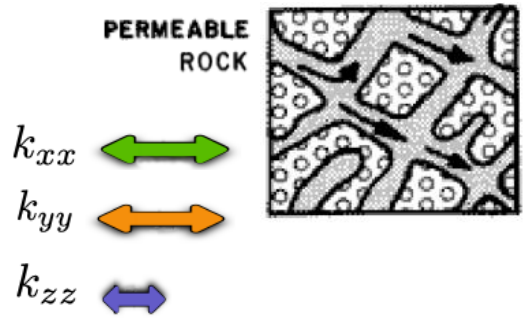


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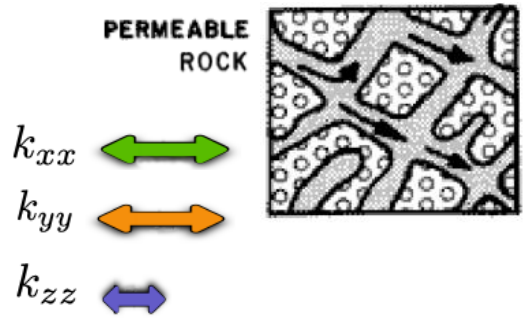
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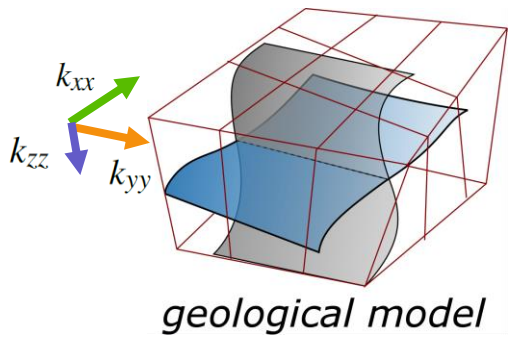


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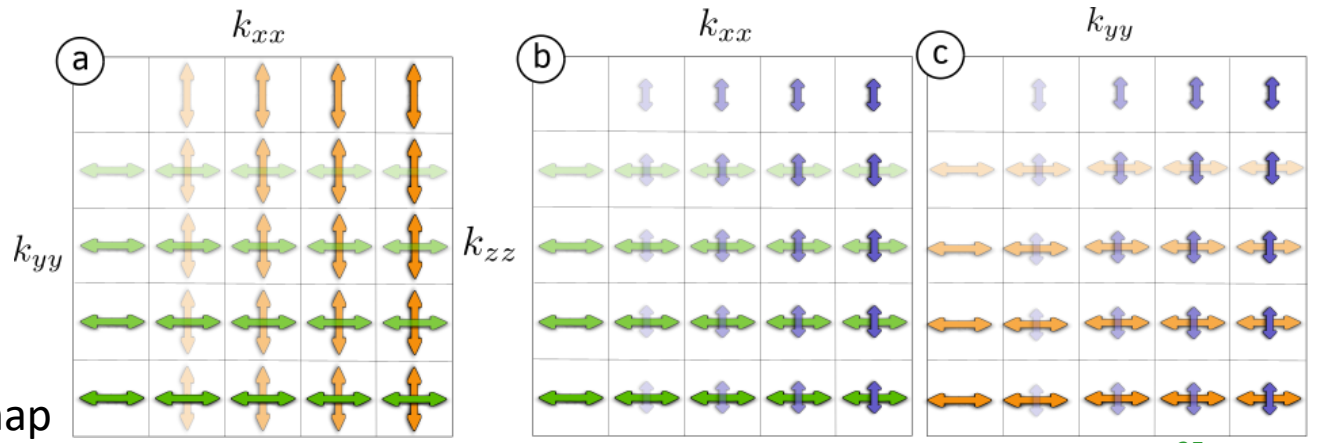
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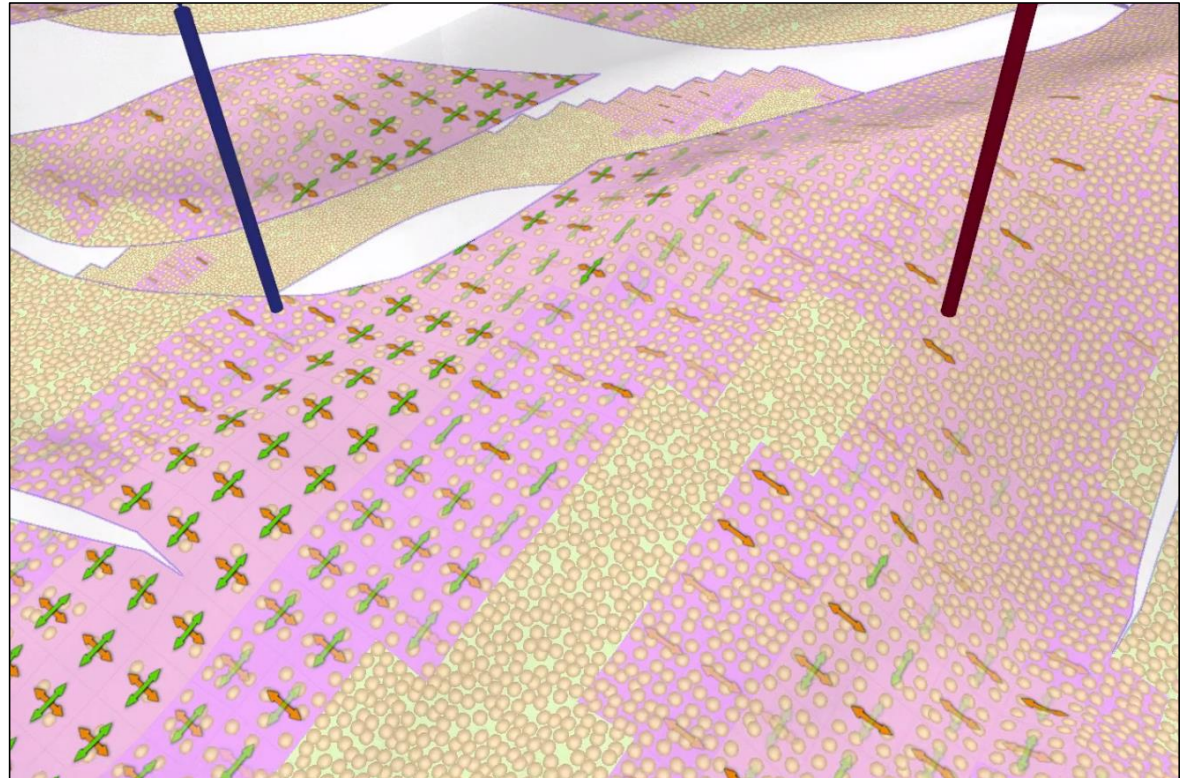


2D decal-map



Visualization Design – Surface layering

- **DG1:** *Suitable representation of geological attributes.*
- **DG2:** *Facilitate communication between multidisciplinary teams.*
- **DG3:** *Facilitate visualization of trends.*
- **DG4:** *Display of multiple attributes*
- **DG5:** *Access the 3D nature of geological models*



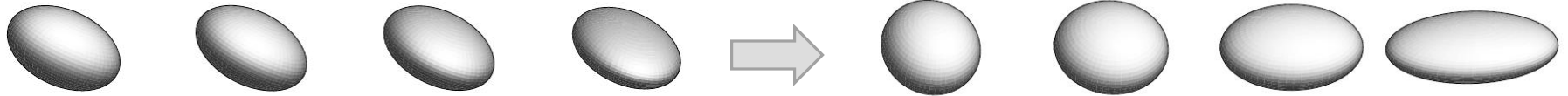


Visualization Design – 3D glyph-based representation

- Rock Permeability (tensor data)
 - Diagonal 3x3 matrix (k_{xx}, k_{yy}, k_{zz})
- Tensor visualization
 - Ellipsoid glyphs $\frac{1}{k_{xx} + k_{yy} + k_{zz}} (k_{xx}, k_{yy}, k_{zz})$

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 - Visual ambiguity problem [Kindlmann, CGF 2004]



Look the same from this point of view

Different point of view

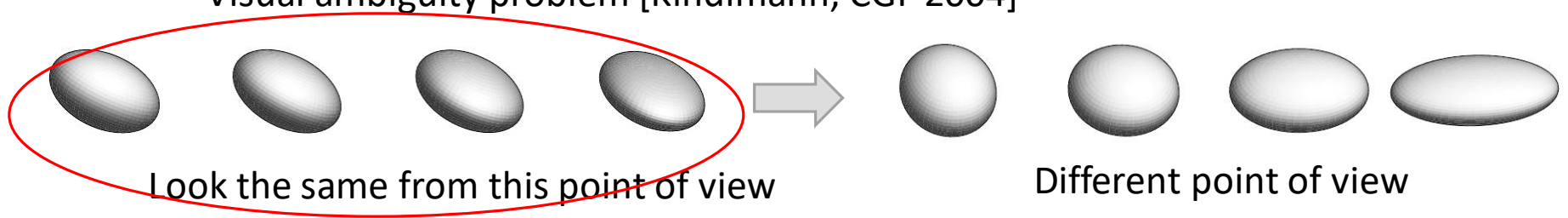


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Shading is not enough to convey orientation

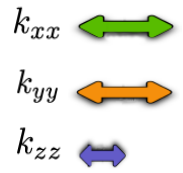
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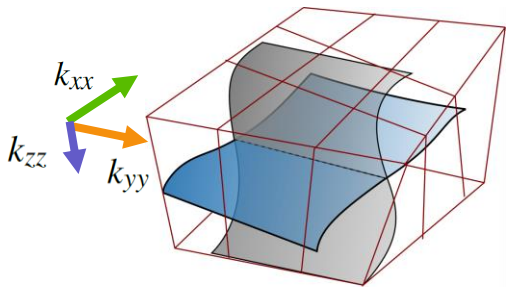


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 - Given a vertex v of the glyph, (ϕ, θ) are given by



$$\theta = \tan^{-1}\left(\frac{v_y}{v_x}\right) \text{ and } \phi = \cos^{-1}\left(\frac{v_z}{\rho}\right), \text{ where } \rho = (v_x + v_y + v_z)^{\frac{1}{2}}$$

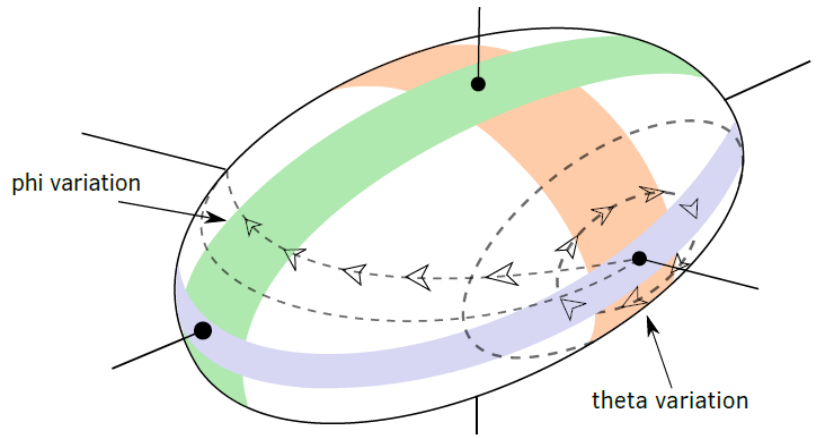


geological model

$$\varepsilon + \frac{\pi}{3} \leq \phi \leq \frac{2\pi}{3} - \varepsilon$$

$$\varepsilon + \frac{4\pi}{3} \leq \phi \leq \frac{5\pi}{3} - \varepsilon$$

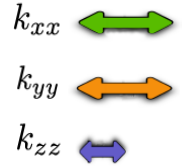
$$0 \leq \theta \leq 2\pi$$



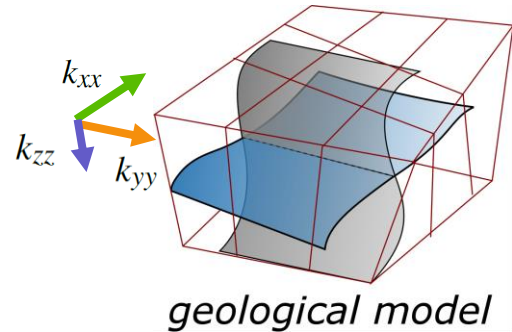


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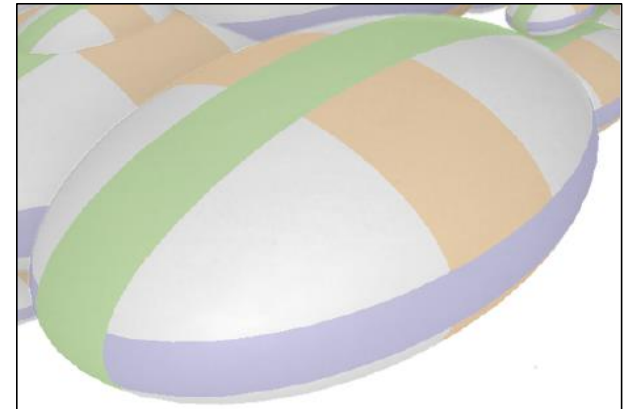
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$$\varepsilon + \frac{\pi}{3} \leq \phi \leq \frac{2\pi}{3} - \varepsilon$$

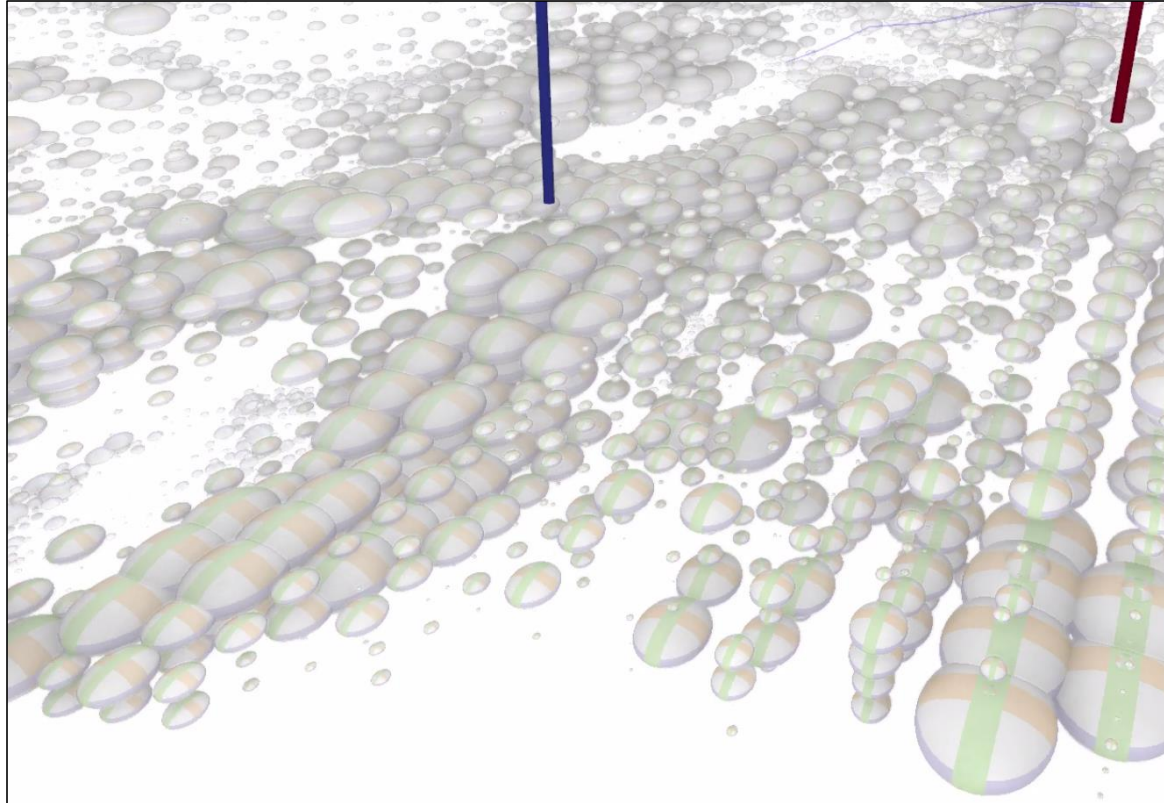
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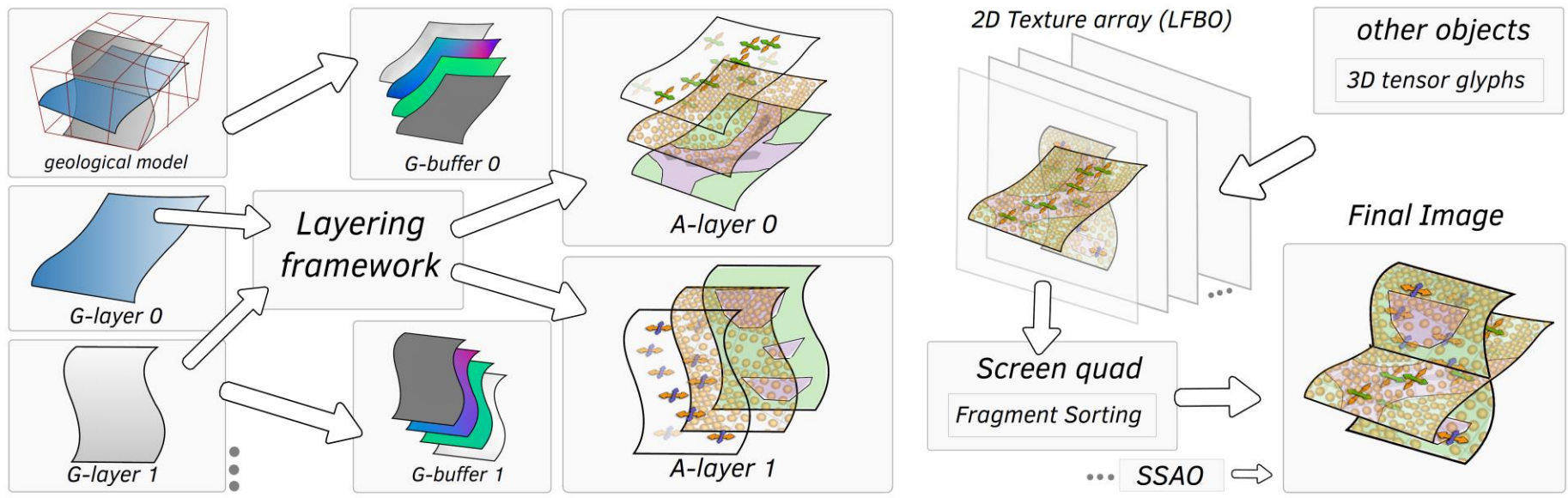
Visualization Design – Surface layering

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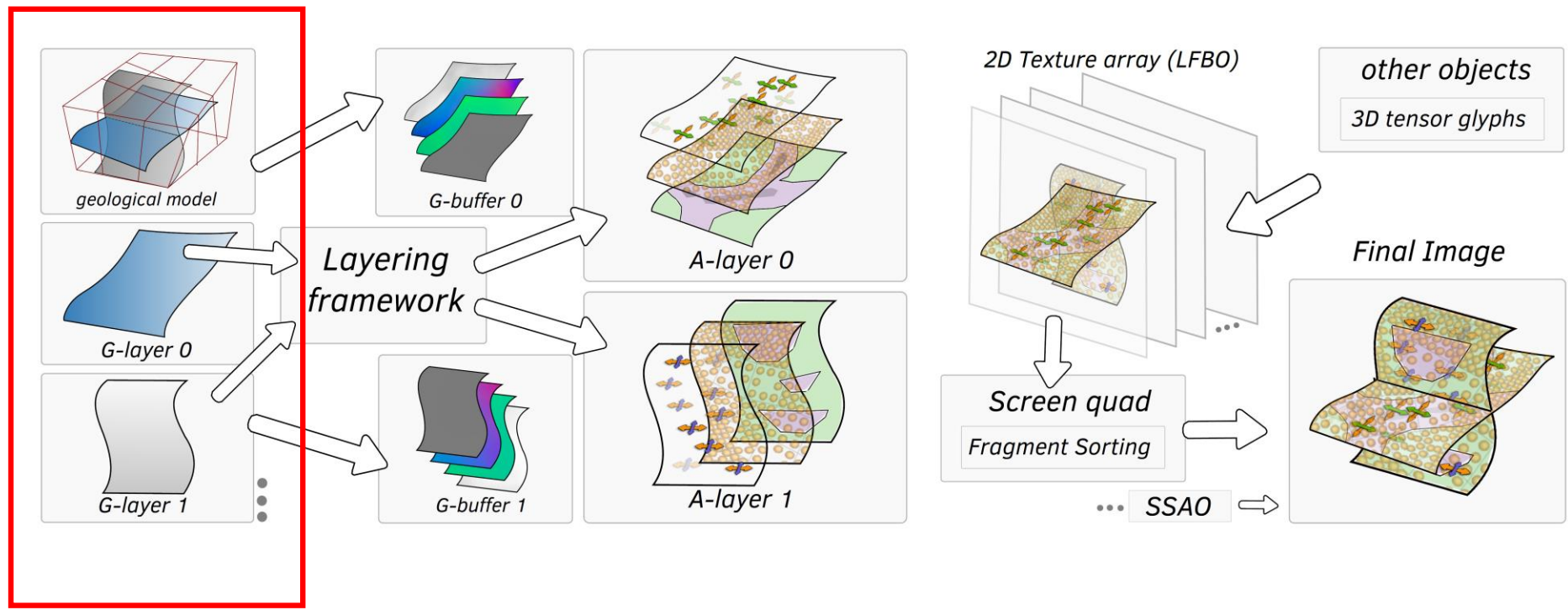
GPU-Implementation - Pipeline



Extending the Layering Pipeline [Rocha *et al.*, 2017]

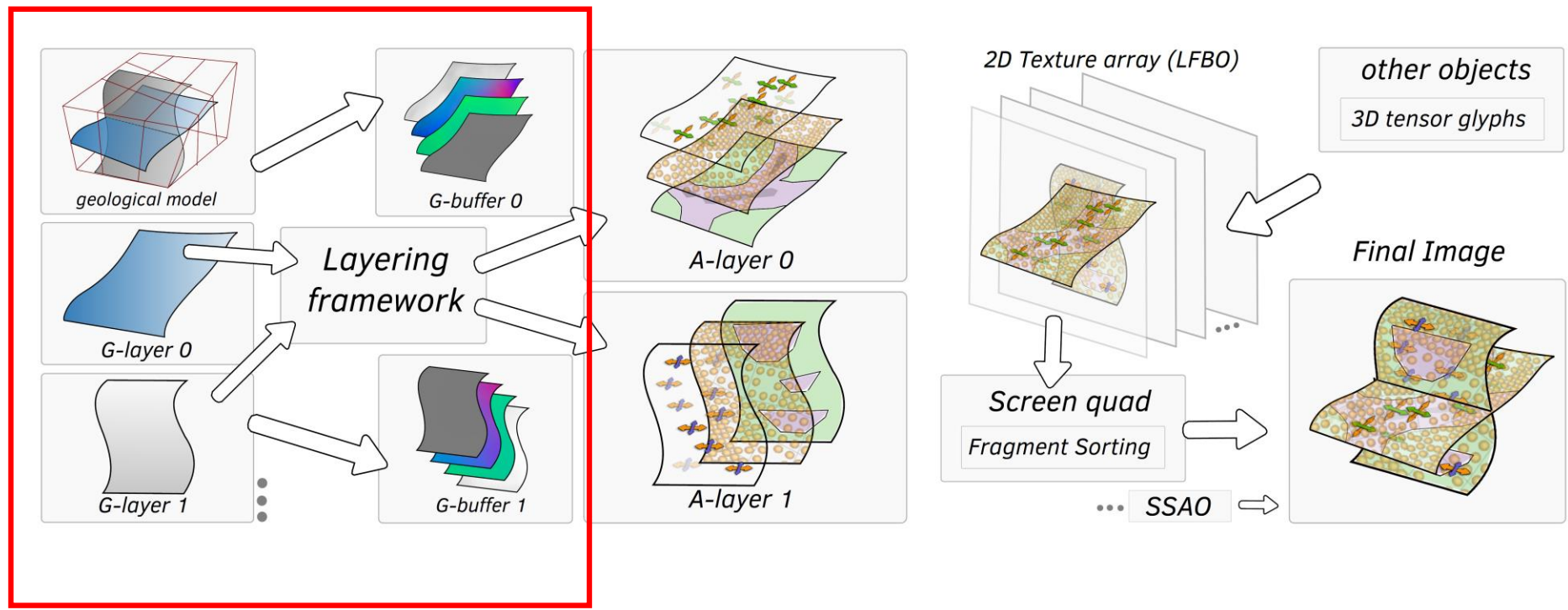


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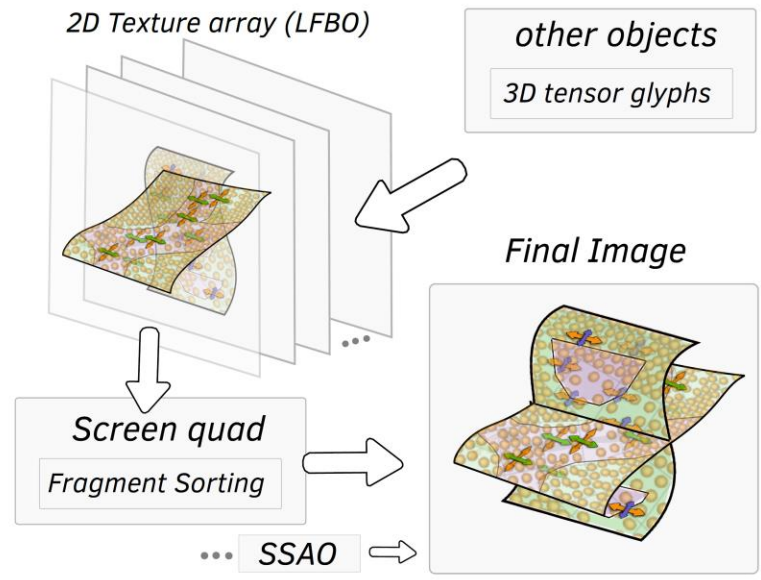
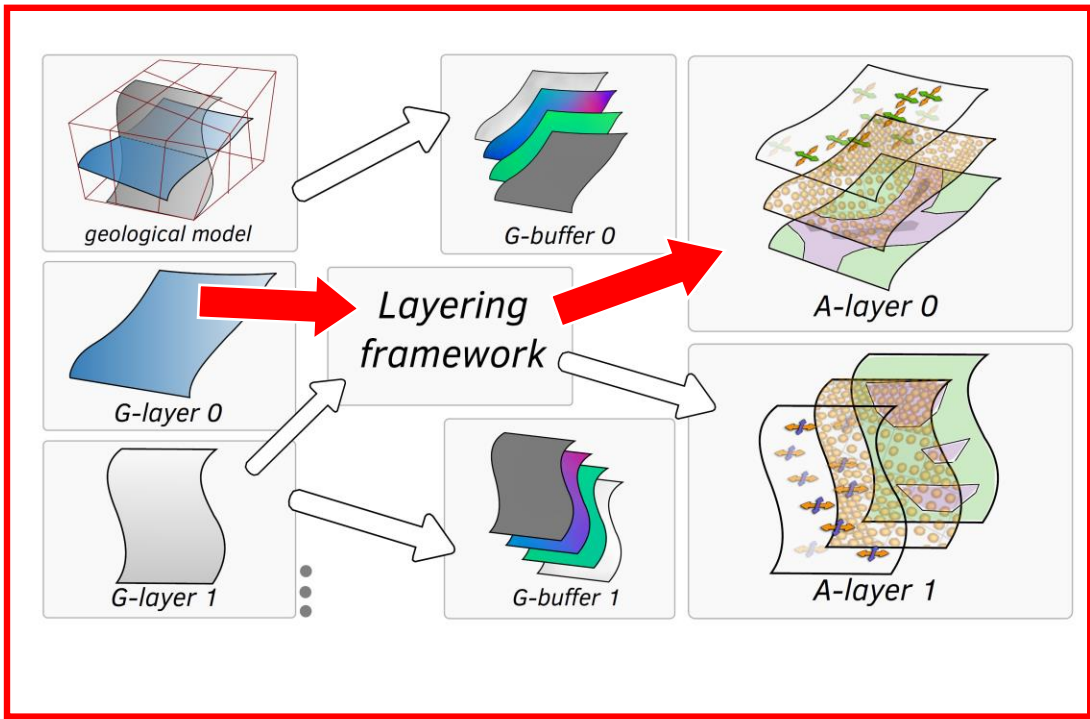


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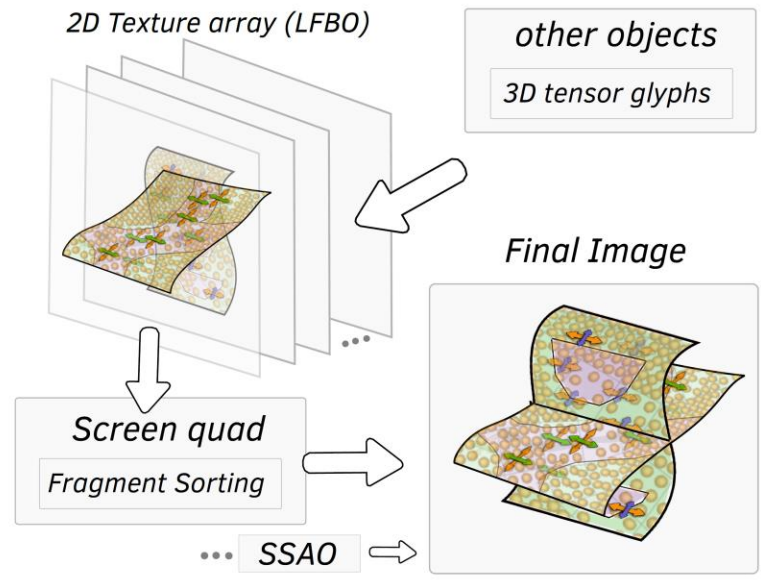
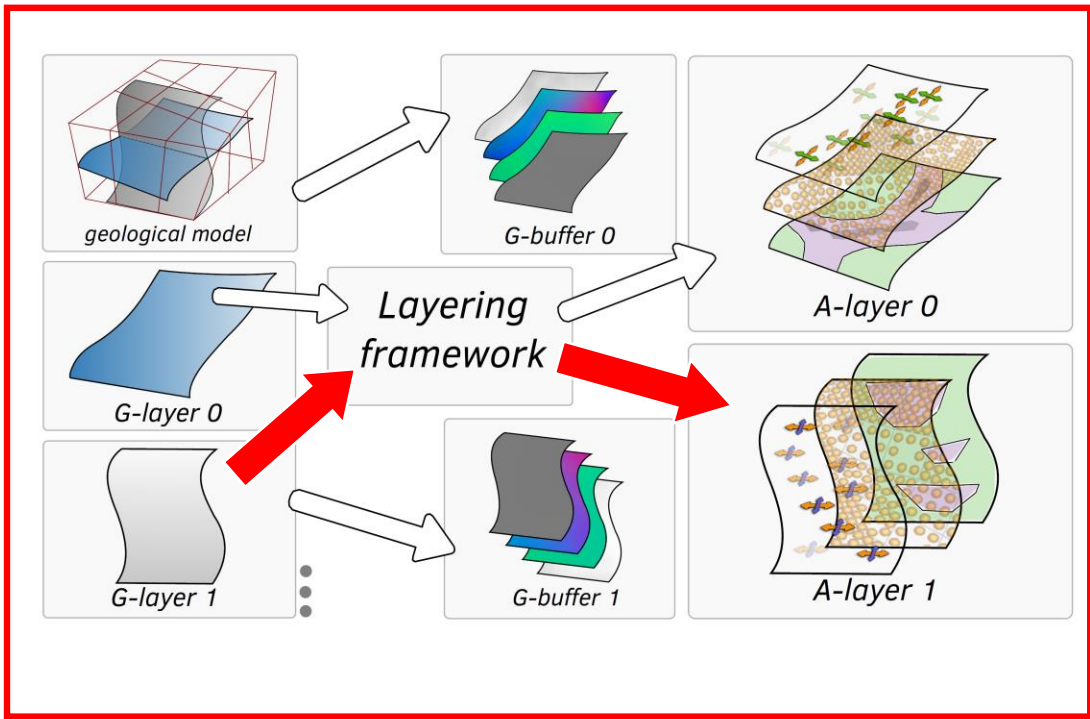


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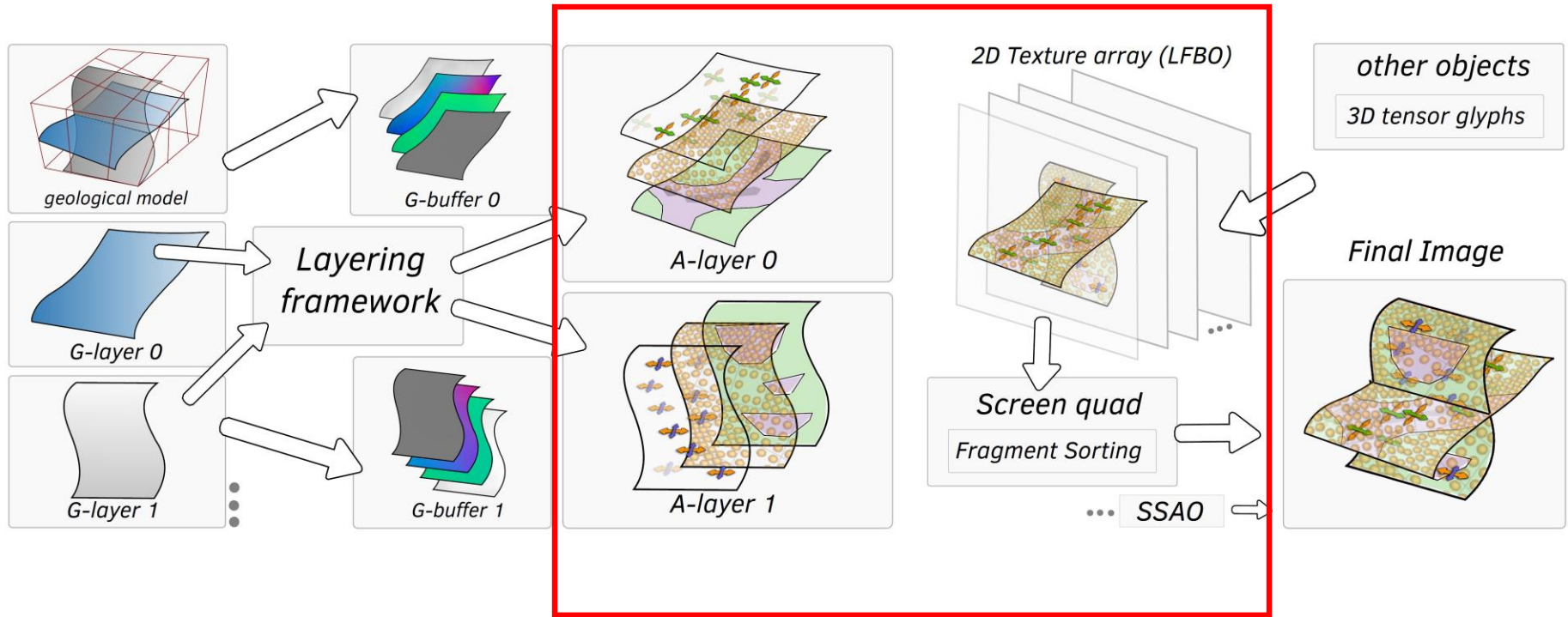


GPU-Implementation - Pipeline



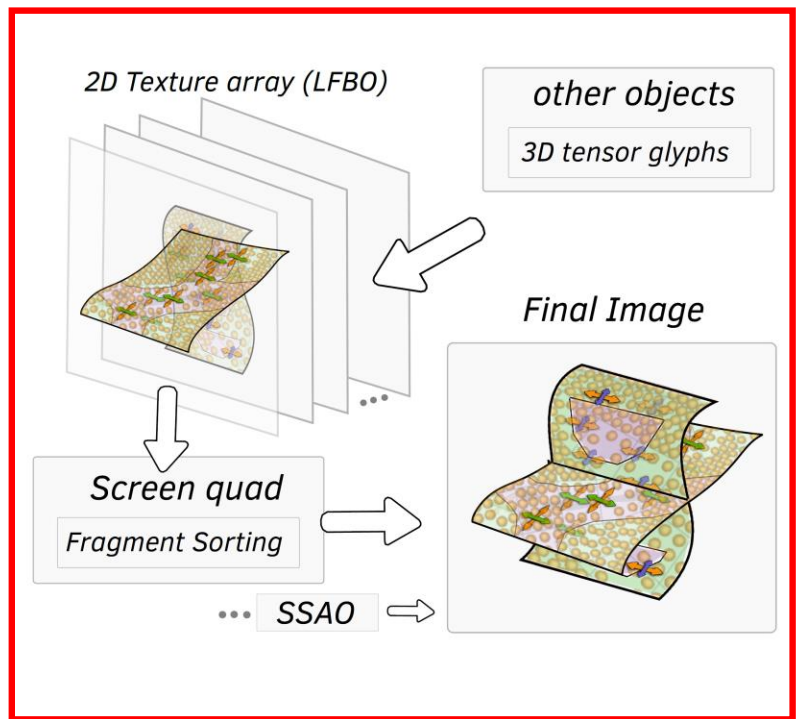
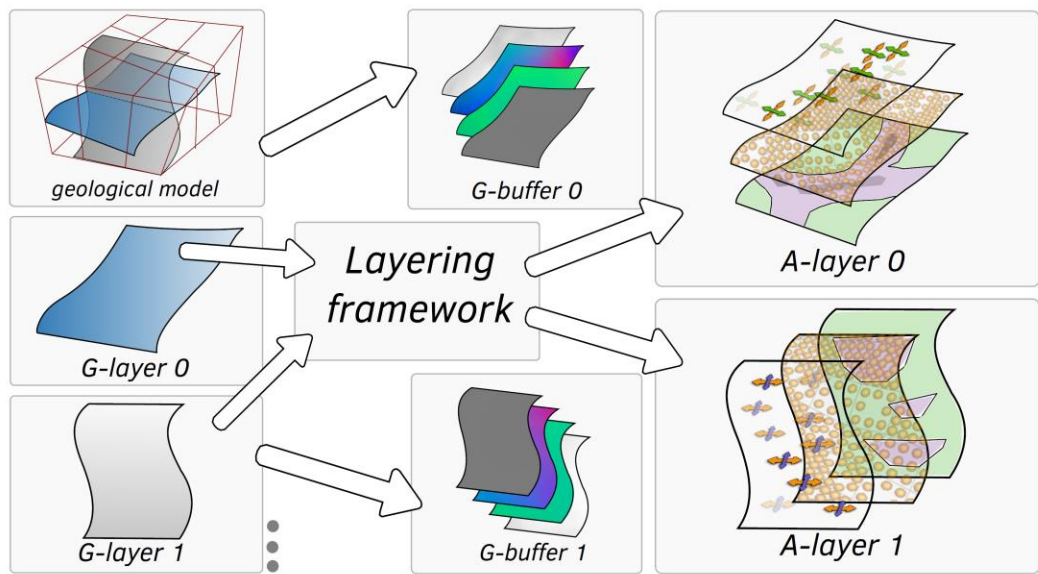


GPU-Implementation - Pipeline



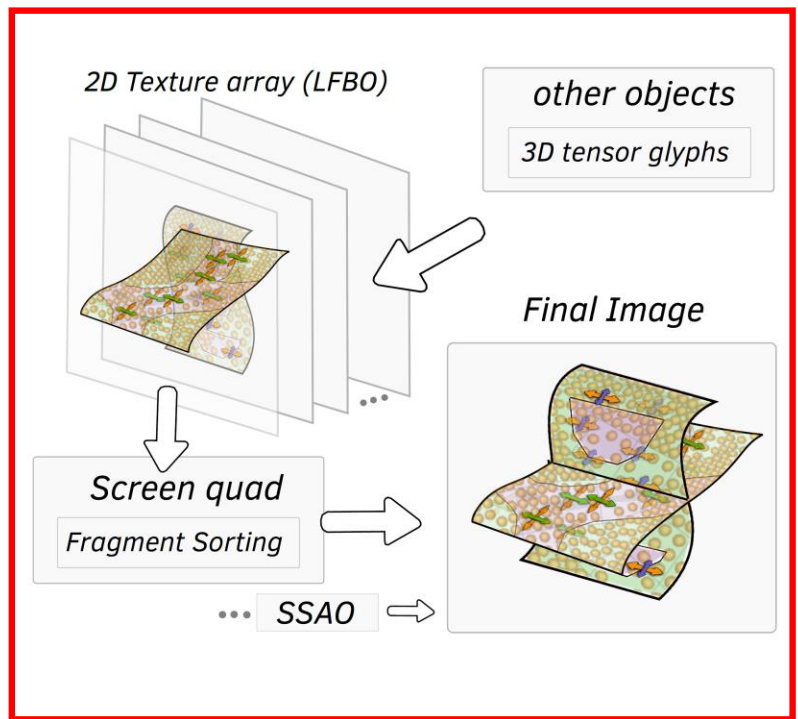
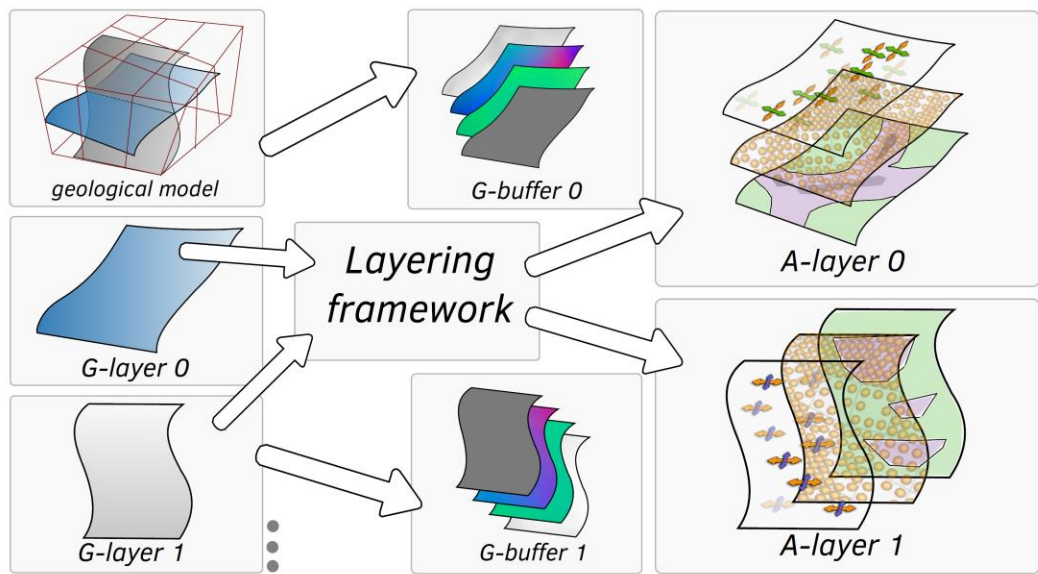


GPU-Implementation - Pipeline



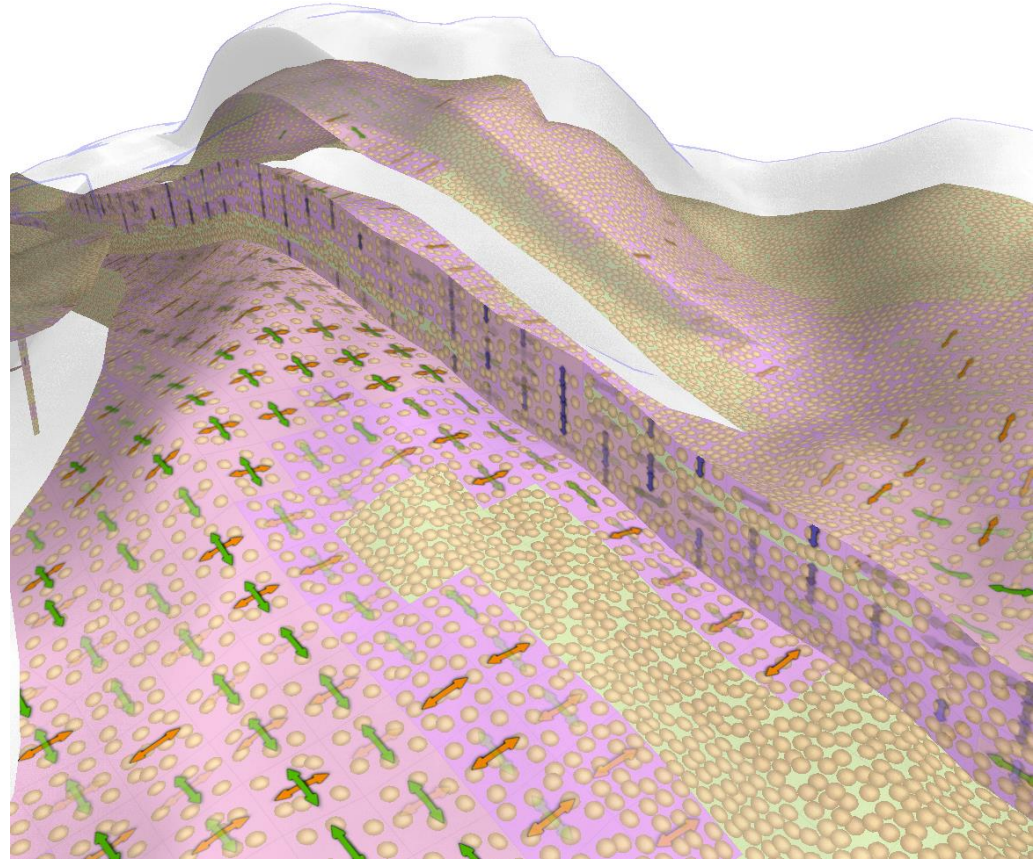


GPU-Implementation - Pipeline



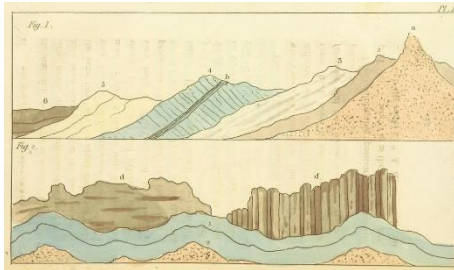
Results

- Illustrative Visualization

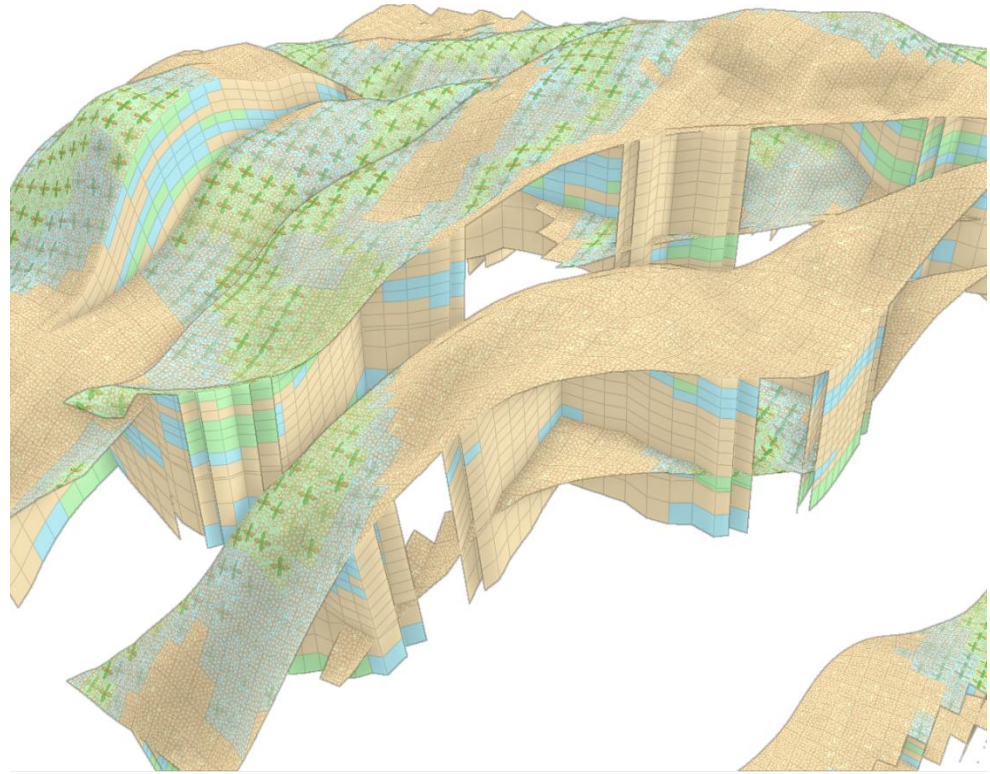


Results

- Illustrative Visualization
- Case Analysis I
- **Case Analysis II**



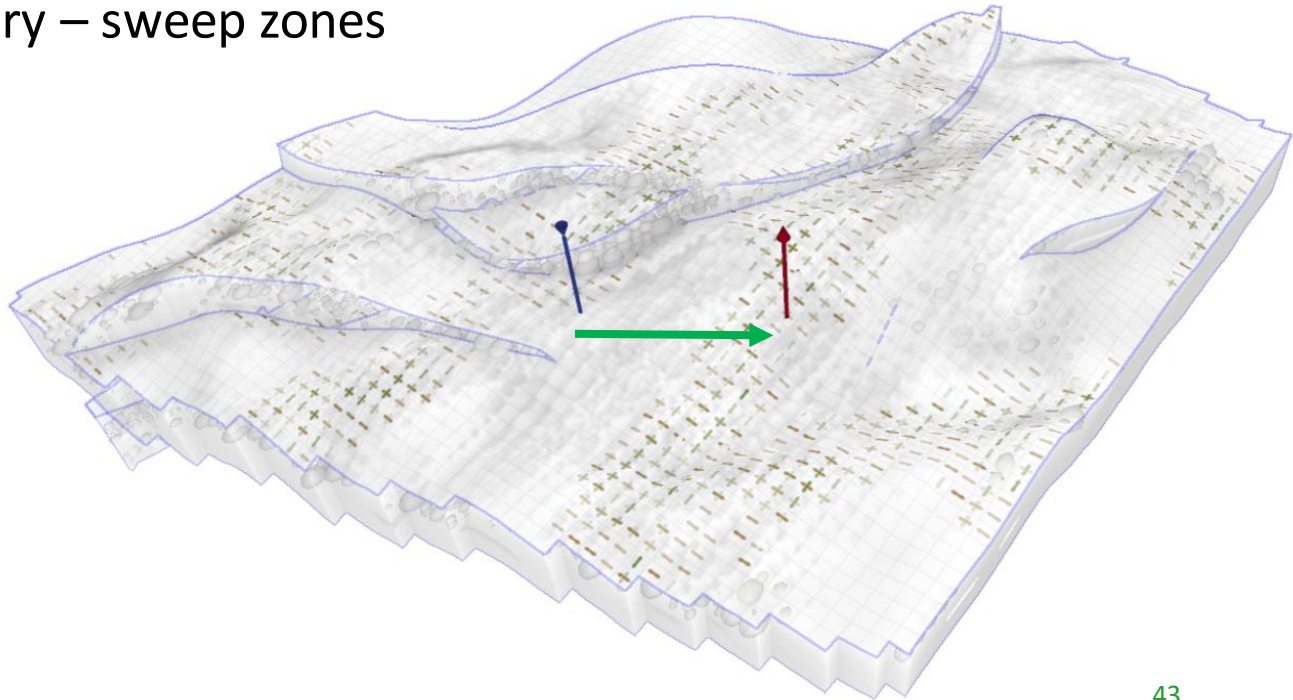
[BAKEWELL R, 1813]





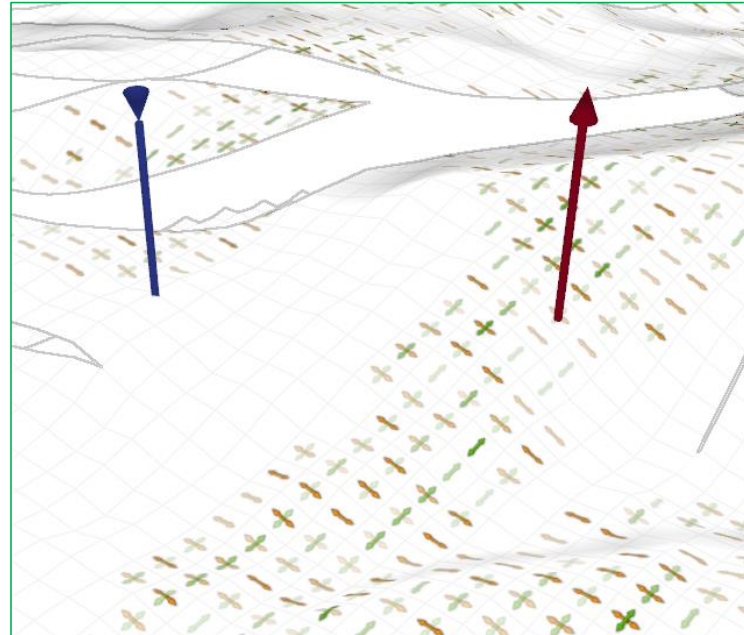
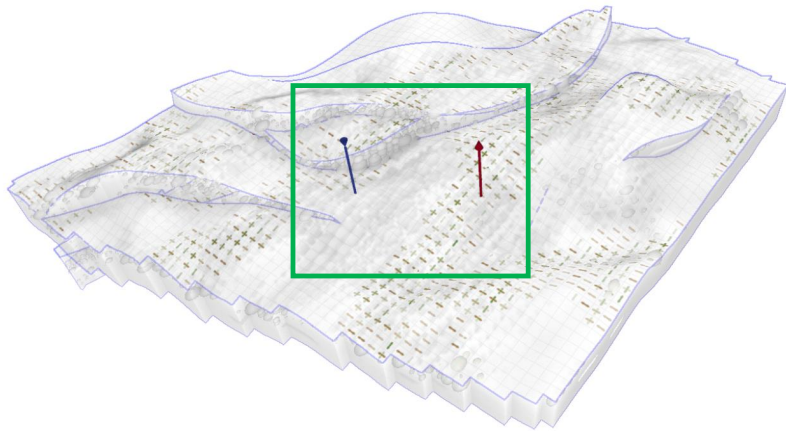
Results – Case Analysis II: Inter-well connectivity

- Connectivity is a fundamental condition for oil drainage
- Secondary recovery – sweep zones



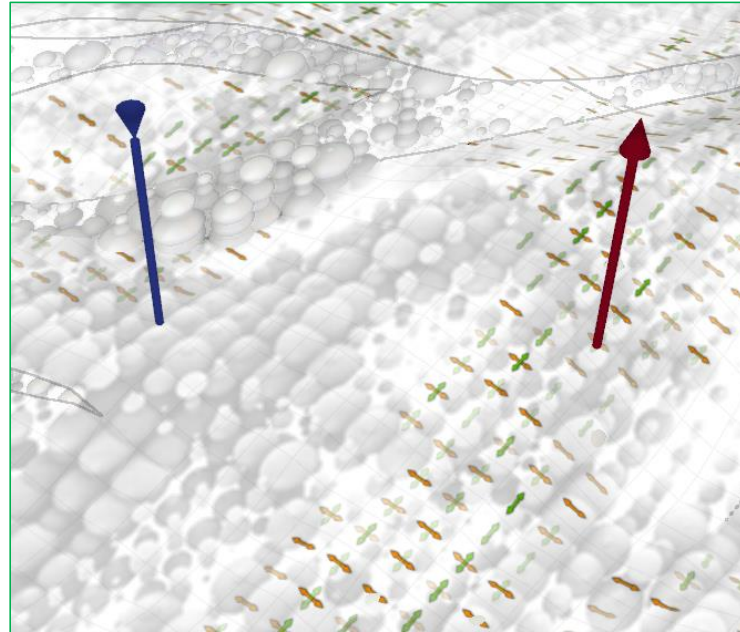
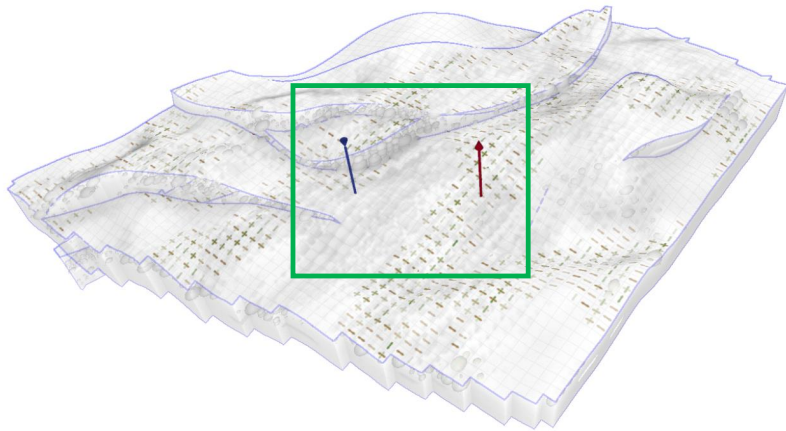
Results – Case Analysis II: Inter-well connectivity

- Evaluating permeability design (decal and tensor)
 - “Can you identify surface areas with low variability of horizontal permeability?” (T1)



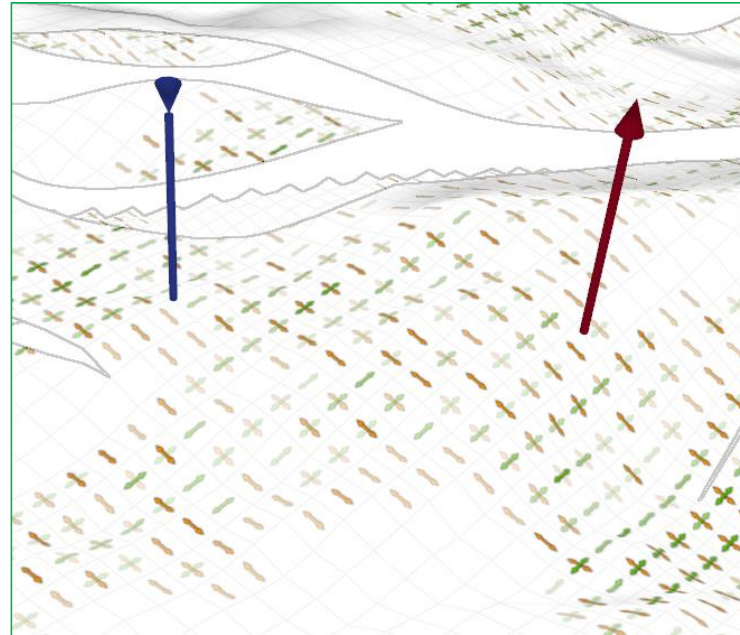
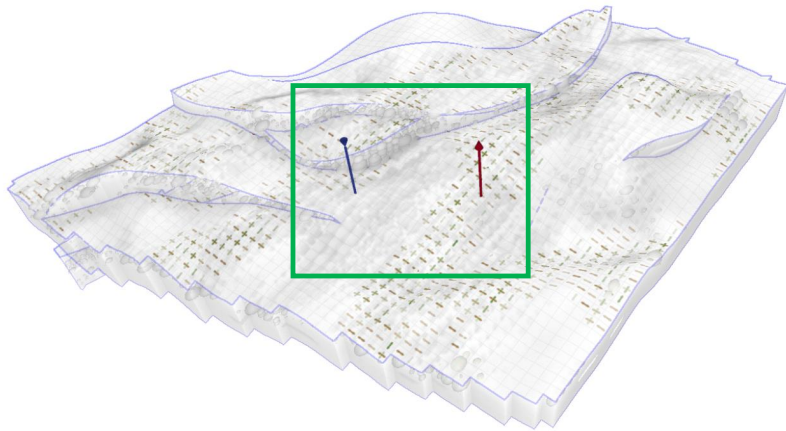
Results – Case Analysis II: Inter-well connectivity

- Evaluating permeability design (decal and tensor)
 - “Can you identify whether the two wells are connected?” (T3)



Results – Case Analysis II: Inter-well connectivity

- Evaluating permeability design (decal and tensor)
 - “I can also more easily compare permeability values in different directions.” (T5)

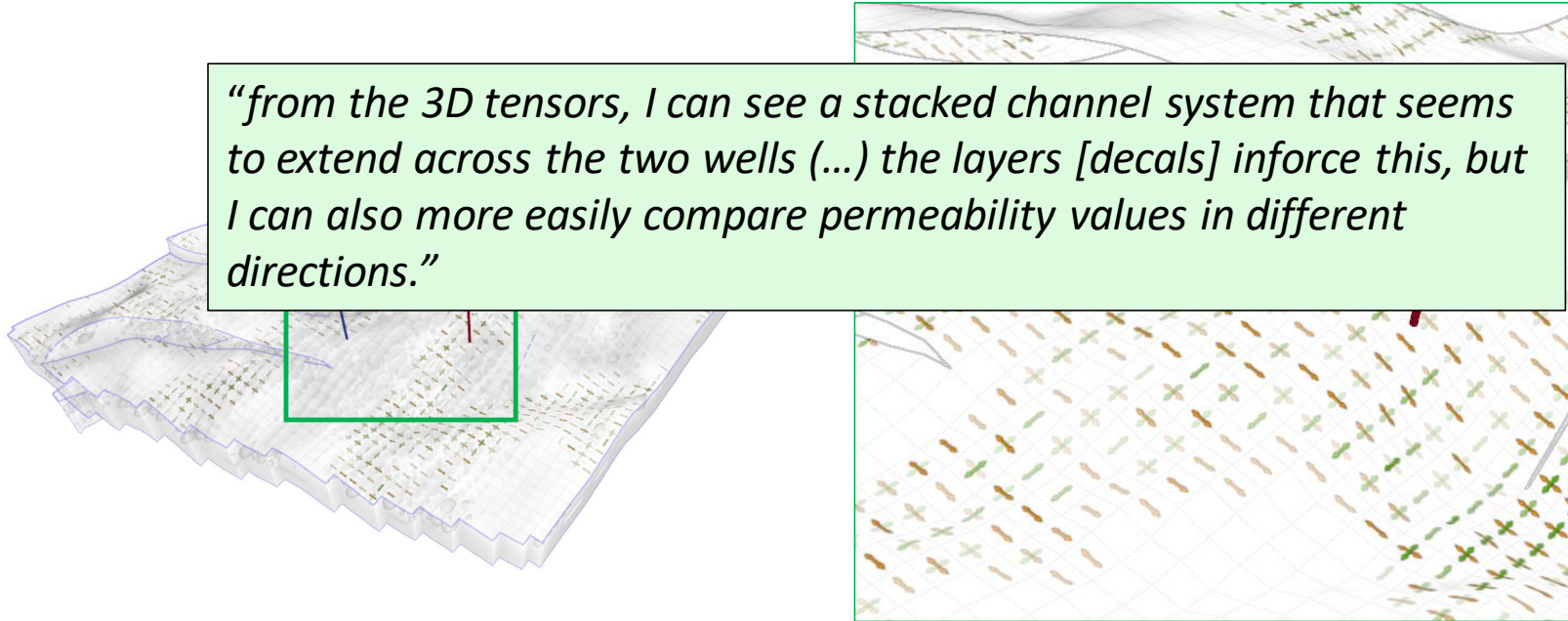




Results – Case Analysis II: Inter-well connectivity

- Evaluating permeability design (decal and tensor)

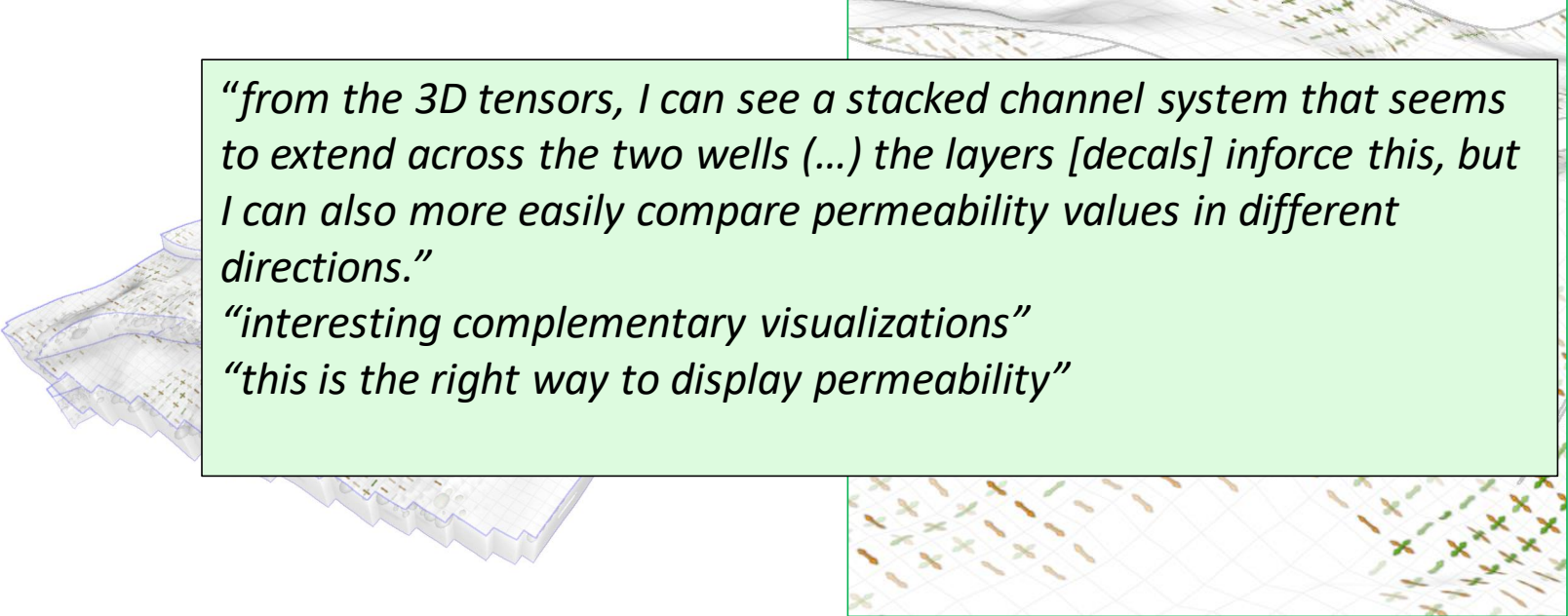
“from the 3D tensors, I can see a stacked channel system that seems to extend across the two wells (...) the layers [decals] inforce this, but I can also more easily compare permeability values in different directions.”





Results – Case Analysis II: Inter-well connectivity

- Evaluating permeability design (decal and tensor)



“from the 3D tensors, I can see a stacked channel system that seems to extend across the two wells (...) the layers [decals] inforce this, but I can also more easily compare permeability values in different directions.”

“interesting complementary visualizations”

“this is the right way to display permeability”



Expert feedback – Case analysis II

- How much impermeable are the cells? (transparency encoding)
- Color-coded bands could be used for additional attributes
- Incorporate suggestions from the experts

More Future Work

- Design space is vast!
- Incorporate new attributes, e.g., water saturation
- On-demand data visualization
- Which new data metaphors can be created using decals?
- Hybrid visualization seems promising



Conclusions - Contributions

- A domain problem characterization to inform visualization practitioners new to this domain
- Multivariate visualization design of multiple geological attributes in a single view
- Surface layering combined with a 3D glyph-based representation.
- A simple importance-sampling method for representing scalar fields
- Extension of the Decal-Maps technique



Thank You!



Illustrative Multivariate Visualization for Geological Modelling

Allan Rocha*, Roberta C. R. Mota*, Hamidreza Hamdi**,
Usman R. Alim*, and Mario Costa Sousa*

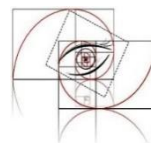
Questions?

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